

## About the solution

Let  $S$  denote the number of different speed limits occurring. It is clear that  $S \leq 500$ . Construct a new graph with  $N * S$  vertices, each one  $(n, v)$  corresponding to the state of being at crossing  $n$  and having speed  $v$ . There is a directed edge from vertex  $(n_1, v_1)$  to vertex  $(n_2, v_2)$  if and only if there is a road  $r$  from crossing  $n_1$  to crossing  $n_2$  and one of the following holds:

1.  $V(r) = v_2$
2.  $V(r) = 0$  and  $v_1 = v_2$

If the weight of the edge is  $L(r) / v_1$ , then the original problem exactly corresponds to finding the shortest path in the new graph from  $(0, 70)$  to  $(D, v)$  with  $v$  arbitrary.

To find the shortest path, Dijkstra's algorithm can be used. The graph does not have to be constructed explicitly. In a typical instance, many of the vertices will not be reached since they have a much longer travel time than the destination. To solve all test cases, a priority queue must be implemented, for example by using a heap or a binary heap.

The test cases distinguish between

1. a recursive solution
2. a clever recursive solution which saves the best path length for given crossing and speed
3. Dijkstra's shortest path with a normal array
4. Dijkstra's shortest path with a priority queue

The maximum number of crossings (150) and velocities (500) are chosen because even the fourth solution starts to take long time ( $\sim 1$  sec) in that region.